Find all triples of natural numbers \( a, b, \) and \( c, \) such that
\[
ab + c = (a^2, b^2) + (a, bc) + (b, ac) + (c, ab) = 239^2
\]
where \((n, m)\) denotes the greatest common divisor of natural numbers \( n \) and \( m.\)