

In all of your answers, make the necessary substitutions so that your results are simplified as much as possible!

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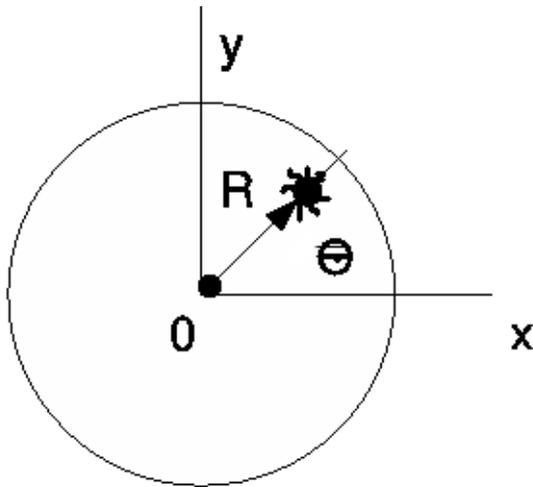


Figure 1: Problem 1

1. (35 points) An insect is walking outwards on a radius of a disk that is rotating with constant speed. Because of the rotation, the the radius makes an angle  $\theta$  with the  $x$ -axis such that  $\theta(t) = \omega t$ , where  $\omega$  is a constant and  $t$  is the time. The distance of the insect from the center is given by  $R(t) = \alpha t$  where  $\alpha$  is another constant.

- (a) What are the units of  $\omega$  and  $\alpha$ ?
- (b) What is the position vector of the insect at time  $t$ ?
- (c) What is the velocity of the insect at time  $t$ ?
- (d) What is the aceleration of the insect at time  $t$ ?

2. (35 points) Atilla is traveling on a train which is moving at 10m/s. Cemal is initially at rest, but then starts running after the train with a constant acceleration of  $g/2$ , where  $g = 10\text{m/s}^2$ . Just when Cemal starts running, Atilla is 10m away, and at that instant Atilla throws a ball in the direction of Cemal, at an angle  $45^\circ$  with respect to the train.

- (a) With what initial speed must Atilla throw the ball so that it will hit Cemal?
- (b) For how much time does the ball fly?
- (c) In which direction is the ball moving with respect to ground?
- (d) How fast is Cemal running when he catches the ball?

3. (30 points) A small body moves along the x axis with constant acceleration according to the equation

$$\frac{dx}{dt} = cx^p,$$

where  $c$  and  $p$  are constants.

Show that the acceleration of the body is

$$a = \frac{1}{2}c^2.$$