

3. In each of the following, if the given statement is true for all continuous functions  $f$  that are defined on  $(-\infty, \infty)$ , then mark the  $\square$  to the left of TRUE with a  $\times$ ; otherwise, mark the  $\square$  to the left of FALSE with a  $\times$  and give a counterexample.

a.  $f$  has a derivative on  $(-\infty, \infty)$ .

TRUE

FALSE, because it does not hold for  $f(x) =$

$|x|$

b.  $f$  has an antiderivative on  $(-\infty, \infty)$ .

TRUE

FALSE, because it does not hold for  $f(x) =$

c.  $\frac{d}{dx} \int_0^1 f(x) dx = f(x)$  for all  $0 \leq x \leq 1$ .

TRUE

FALSE, because it does not hold for  $f(x) =$

$1$

d. If  $f$  is increasing on  $(-\infty, \infty)$ , then  $f^2$  is increasing on  $(-\infty, \infty)$ .

TRUE

FALSE, because it does not hold for  $f(x) =$

$x$

e. If  $f$  is decreasing on  $(-\infty, \infty)$ , then  $e^f$  is decreasing on  $(-\infty, \infty)$ .

TRUE

FALSE, because it does not hold for  $f(x) =$