

## MATH101: HOMEWORK IV: Spring 2011

### For all Sections

(Due April 18th week: first hour of the second lecture day)

#### QUESTIONS:

1. Evaluate the following indefinite integrals:

(1.a)

$$\int \frac{1}{x^3} \sqrt{\frac{1-x^2}{x^2}} dx$$

(1.b)

$$\int \frac{dy}{\sqrt{e^{2y} - 1}}$$

2. Evaluate the following definite integrals:

(2.a)

$$\int_0^{\pi/4} \pi^{\tan x} \sec^2 x dx$$

(2.b) Show that

$$2 \leq \int_{-1}^1 \sqrt{1+x^2} dx \leq 2\sqrt{2}$$

3. (3.a) Find the area of the region in the first quadrant bounded on the left by the  $y$ -axis, below by the curve  $x = 2\sqrt{y}$ , above left by the curve  $x = (y-1)^2$ , and above right by the line  $x = 3 - y$  (*This is from the text book, page 352, problem 106*). (3.b) Graph the function

$$f(x) = \begin{cases} \sqrt{1-x}, & 0 \leq x < 1 \\ (7x-6)^{-1/3}, & 1 \leq x \leq 2 \end{cases}$$

and integrate it over its domain.

4. (4.a) Find the limit  $\lim_{n \rightarrow \infty} \left( \frac{n}{n^2+1} + \frac{n}{n^2+4} + \cdots + \frac{n}{n^2+k^2} + \cdots + \frac{n}{2n^2} \right)$ . (4.b) Find the volume of the following solid: The base of the solid is the disk  $x^2 + y^2 \leq 1$ . The cross-sections by the planes perpendicular to the  $y$ -axis between  $y = -1$  and  $y = 1$  are isosceles right triangles with one leg in the disk.

5. (5.a) Find the area between the curves  $y^2 - x - 4y = 0$  and  $y^2 + x - 2y = 0$ . (5.b) Find the volume of the solid obtained by rotating the region bounded by  $y = x - x^2$  and  $y = 0$  about the line  $x = 2$ .