# ODTU-Bilkent Algebraic Geometry 

# Monotonicity of the Hilbert Functions of some monomial curves 

## By

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Abstract: Let $\$ S \$$ be a 4 -generated pseudo-symmetric semigroup generated by the positive integers $\left.\$ \backslash\left\{n \_1, n \_2, n \_3, n \_4\right\}\right\} \$$ where $\$ \operatorname{lgcd}\left(n \_1, n \_2, n \_3, n \_4\right)$ $=1 \$$. $\$ k \$$ being a field, let $\$ k[S] \$$ be the corresponding semigroup ring and
\$I_S\$ be the defining ideal of $\$ \mathbf{S} \$$. \$f_* being the homogeneous summand of $\$ \$ \$$, tangent cone of $\$ S \$$ is $\$ k[S] /\left\{I \_S\right\}_{-}^{*} \$$ where $\$\left\{I \_S\right\}{ }^{*}=<f_{-}^{*}|f|$ in $I \_S>\$$. We will show that the "Hilbert function of the local ring (which is isomorphic to the tangent cone) for a 4 generated pseudo-symmetric numerical semigroup \$<n_1,n_2,n_3,n_4>\$ is always non-decreasing when \$n_1<n_2<n_3<n_4\$" by an explicit Hilbert function computation.

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Time: 15:40 (GMT+3)
Place: Zoom

