Bilkent University
Department of Mathematics

PROBLEM OF THE MONTH

Term: September 2022

For a given positive integer n, let $f(n)$ be the smallest *positive* number which can be expressed as

$$\frac{ab}{a+b} - n$$

where a and b are positive integers. Find a closed form for $f(n)$ as a function of n.