



Bilkent University
Department of Mathematics

PROBLEM OF THE MONTH

Term: December 2021

Find all primes p for which there exist an odd integer n and a polynomial $Q(x)$ with integer coefficients such that the polynomial

$$1 + pn^2 + \prod_{i=1}^{2p-2} Q(x^i)$$

has at least one integer root.