



Bilkent University  
Department of Mathematics

## PROBLEM OF THE MONTH

**Term:** January 2019

Graphistan has 2019 cities and Graph Air (GA) is running one-way flights between all pairs of these cities. Determine the maximum possible value of the integer  $k$  such that no matter how these flights are arranged it is possible to travel from any city to any other city in Graphistan riding only GA flights so long as the absolute values of the difference between the number of flights originating and terminating at any city is not more than  $k$ .