Problem Of The Month

Term: January 2014

All unit squares of 2014 $\times$ 2014 grid $A$ are colored either white or black. Consider all 2014! colored grids obtained from $A$ by all possible column permutations. What is the maximal possible number of distinctly colored main diagonals (diagonals starting at the lowest unit square of the leftmost column)?