Problem Of The Month

Term: January 2007

Find the greatest common divisor of natural numbers $a$ and $b$ satisfying

$$(1 + \sqrt{2})^{2007} = a + b\sqrt{2}.$$