## **Bilkent University, Department of Physics**

## PHYS 453: Nuclear & Particle Physics

## **First Midterm Examination**

Duration: 70 minutes

**Date:** 9 March 2012

1. (20 points) A particle travelling at speed u approaches an identical particle at rest (in the Lab frame).

a) Show that the speed of each particle in the CM frame is  $\frac{c^2}{u} \left(1 - \sqrt{1 - \frac{u^2}{c^2}}\right)$ ,

- b) Work out the non-relativistic limit of part (a).
- 2. (15 points) An atom of mass m is at rest in the Lab frame. It emits a photon of frequency  $\nu$  after which it suffers a recoil while its mass reduces to  $m \delta m$ . Show that

$$h\nu = c^2 \delta m \left(1 - \frac{\delta m}{2m}\right).$$

3. (15 points) If a quark, which is spin-1/2, is in the *p* orbital angular momentum state (i.e., L=1),

a) What are the possible values for total angular momenta and their z-components,  $|JM\rangle$ ?

b) If this quark is in the total angular momentum state of +1/2, with its z-projection -1/2, What values might we get for the measurement of the z-component of the orbital angular momentum,  $L_z$ , and with what probabilities for each?

NB: All angular momenta are specified in units of  $\hbar$ .

## Some Information (may or may not be useful):

- For  $x \ll 1, (1+x)^a \simeq 1 + ax$ .
- $v_{AC} = \frac{v_{AB} + v_{BC}}{1 + \frac{v_{AB} + v_{BC}}{c^2}}$
- $\gamma = \frac{1}{\sqrt{1-\beta^2}}, \ \beta = \frac{v}{c}$
- For massive particles,  $p_{\mu}p^{\mu} = m^2c^2$ ,  $p_{\mu} = (\frac{E}{c}, \vec{p}), \ \vec{p} = \gamma m\vec{v}$
- For massless particles,  $E = |\vec{p}| c$
- Flip the page for the Clebsch-Gordan coefficient Table



Figure 36.1: The sign convention is that of Wigner (*Group Theory*, Academic Press, New York, 1959), also used by Condon and Shortley (*The Theory of Atomic Spectra*, Cambridge Univ. Press, New York, 1953), Rose (*Elementary Theory of Angular Momentum*, Wiley, New York, 1957), and Cohen (*Tables of the Clebsch-Gordan Coefficients*, North American Rockwell Science Center, Thousand Oaks, Calif., 1974).