

5. Let $E = \{(x, y, z) : x^2 + y^2 \leq 3, 0 \leq x \leq y, \text{ and } 0 \leq z \leq 3\}$.

a. Fill in the boxes so that the following equality holds for all continuous functions f where (x, y, z) are the rectangular coordinates.

$$\iiint_E f(x, y, z) dV = \int_0^{\sqrt{3}} \int_{-\sqrt{3-x^2}}^{\sqrt{3-x^2}} \int_0^3 f(x, y, z) dz dy dx$$

b. Fill in the boxes so that the following equality holds for all continuous functions f where (r, θ, z) are the cylindrical coordinates.

$$\iiint_E f(x, y, z) dV = \int_{\pi/4}^{\pi/2} \int_0^{\sqrt{3}} \int_0^3 f(r \cos \theta, r \sin \theta, z) r dz dr d\theta$$

c. Fill in the boxes so that the following equality holds for all continuous functions f where (ρ, ϕ, θ) are the spherical coordinates.

$$\iiint_E f(x, y, z) dV$$

$$= \int_{\pi/4}^{\pi/2} \int_0^{\pi/6} \int_0^{3/\cos \phi} f(\rho \sin \phi \cos \theta, \rho \sin \phi \sin \theta, \rho \cos \phi) \rho^2 \sin \phi d\rho d\phi d\theta$$

$$+ \int_{\pi/4}^{\pi/2} \int_{\pi/6}^{\pi/2} \int_0^{\sqrt{3}/\sin \phi} f(\rho \sin \phi \cos \theta, \rho \sin \phi \sin \theta, \rho \cos \phi) \rho^2 \sin \phi d\rho d\phi d\theta$$

