

Bilkent University Department of Mathematics

PROBLEM OF THE MONTH

Term: September 2013

Show that for all positive real numbers $a,\ b,\ c$ satisfying a+b+c=1 the following inequality is held:

$$\frac{a^4 + 5b^4}{a(a+2b)} + \frac{b^4 + 5c^4}{b(b+2c)} + \frac{c^4 + 5a^4}{c(c+2a)} \ge 1 - ab - bc - ca$$