

Bilkent University
Department of Mathematics

## Problem Of The Month

Term: March 2012

We say that a rational number $r \in(0,1)$ is $n$-good if the decimal expansion of $r$ is: $r=0 . r_{1} r_{2} \ldots, r_{n}$ and $r_{i} \neq 9$ for all $i=1,2, \ldots, n$. Let $G_{n}$ be the set off all $n$-good numbers. Find the limit

$$
\lim _{n \rightarrow \infty} \frac{\left|G_{n}\right|}{S_{n}}
$$

where $\left|G_{n}\right|$ is the number of elements in $G_{n}$ and $S_{n}$ is the sum of all elements of $G_{n}$.

