

Bilkent University Department of Mathematics

PROBLEM OF THE MONTH

Term: March 2012

We say that a rational number $r \in (0,1)$ is n-good if the decimal expansion of r is: $r = 0.r_1r_2...,r_n$ and $r_i \neq 9$ for all i = 1,2,...,n. Let G_n be the set off all n-good numbers. Find the limit

$$\lim_{n\to\infty}\frac{|G_n|}{S_n}$$

where $|G_n|$ is the number of elements in G_n and S_n is the sum of all elements of G_n .